CSC 533: Programming Languages

Spring 2016

Scheme structures

- memory management: structure sharing, garbage collection
- structuring data: association list, trees
- let expressions
- non-functional features: set!, read, display, begin

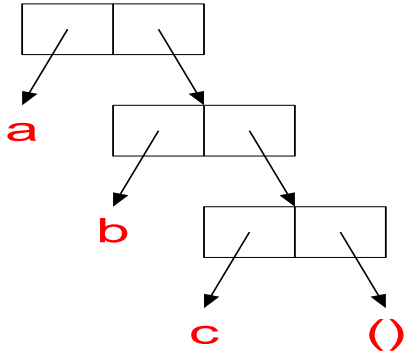
Memory management in Scheme

all data is dynamically allocated (heap-based)

- variables (from function definitions, let-expressions) may be stored on stack

underlying lists is the dotted-pair structure

```
(a b c)  ≡  (a . (b . (c . ())))
```



this structure demonstrates

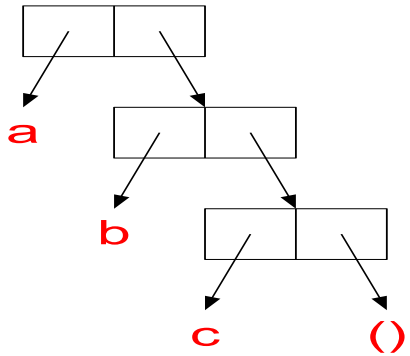
- non-contiguous nature of lists (non-linear linked-lists)
- behavior of primitive operations (car, cdr, cons)

```
(car '(a b c)) ≡ (car '(a . (b . (c . ())))) → a

(cdr '(a b c)) ≡ (cdr '(a . (b . (c . ())))) → (b . (c . ())) ≡ (b c)

(cons 'x '(a b c)) ≡ (cons 'x '(a . (b . (c . ()))))
                   → (x . (a . (b . (c . ())))) ≡ (x a b c)
```

Structure sharing

since destructive assignments are rare, Scheme makes extensive use of structure-sharing

```
(define (my-length lst)
  (if (null? lst)
      0
      (+ 1 (my-length (cdr lst)))))

➢ (my-length '(a b c))
3
```



- each recursive call shares a part of the list
- other code that uses `a`, `b`, `c` or `()` can share as well

problems caused by destructive assignments? solutions?

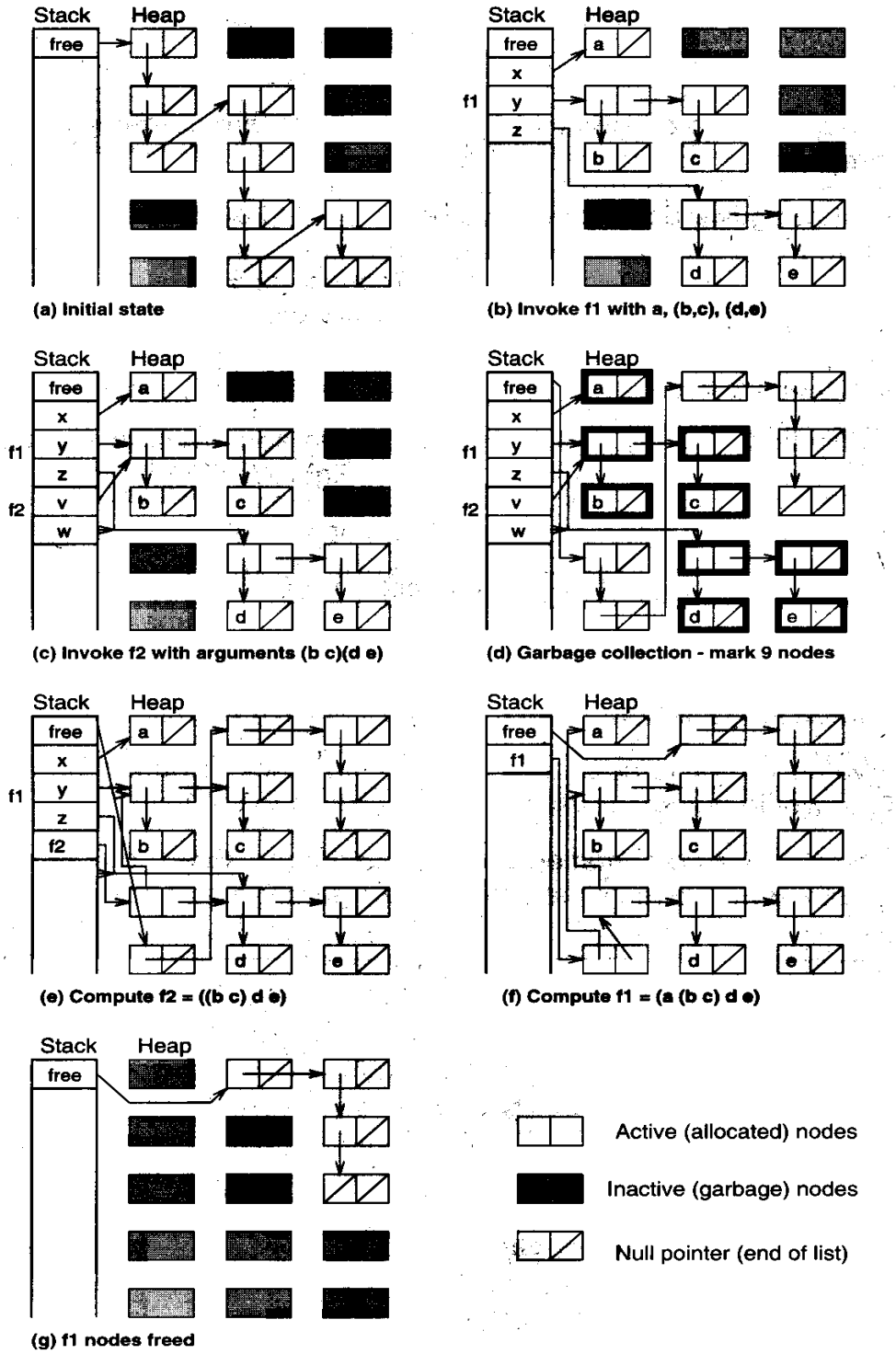
Garbage collection

garbage collection is used to reclaim heap memory

```
(define (f1 x y z)
  (cons x (f2 y z)))

(define (f2 v w)
  (cons v w))
```

➢ `(f1 'a '(b c) '(d e))`

`(a (b c) d e)`



Structuring data

an association list is a list of "records"

- each record is a list of related information, keyed by the first field
- i.e., a Map

```
(define NAMES '((Smith Pat Q)
                (Jones Chris J)
                (Walker Kelly T)
                (Thompson Shelly P)))
```

note: can use `define` to create "global constants" *(for convenience)*

- can access the record (sublist) for a particular entry using `assoc`

```
➢ (assoc 'Smith NAMES)
(Smith Pat Q)
```

```
➢ (assoc 'Walker NAMES)
(Walker Kelly T)
```

- `assoc` traverses the association list, checks the `car` of each sublist

```
(define (my-assoc key assoc-list)
  (cond ((null? assoc-list) #f)
        ((equal? key (caar assoc-list)) (car assoc-list))
        (else (my-assoc key (cdr assoc-list)))))
```

Association lists

to access structured data,

- store in an association list with search key first
- access via the search key (using assoc)
- use car/cdr to select the desired information from the returned record

```
(define MENU '((bean-burger 2.99)
               (tofu-dog 2.49)
               (fries 0.99)
               (medium-soda 0.79)
               (large-soda 0.99)))
```

```
➢ (cadr (assoc 'fries MENU))
0.99
```

```
➢ (cadr (assoc 'tofu-dog MENU))
2.49
```

```
(define (price item)
  (cadr (assoc item MENU)))
```

`assoc` example

consider a more general problem: determine price for an entire meal

- represent the meal order as a list of items,

  e.g., `(tofu-dog fries large-soda)`

- use recursion to traverse the meal list, add up price of each item

```
(define (meal-price meal)
  (if (null? meal)
      0.0
      (+ (price (car meal)) (meal-price (cdr meal)))))
```

- alternatively, could use `map` & `apply`

```
(define (meal-price meal)
  (apply + (map price meal)))
```

In-class exercise

given a menu structure:

```
(define MENU '((bean-burger 2.99)
               (tofu-dog 2.49)
               (fries 0.99)
               (medium-soda 0.79)
               (large-soda 0.99)))
```

define a function to count how many items are below a certain price

```
(define (numPricedBelow price menu)
    ??? )
```

```
(numPricedBelow 1.00 MENU) → 3

(numPricedBelow 0.99 MENU) → 1
```

Finally, variables!

Scheme does provide for variables and destructive assignments

```
➢ (define x 4)
➢
➢ x
4
➢ (set! x (+ x 1))
➢
➢ x
5
```

`define` creates and initializes a variable

`set!` updates a variable

since Scheme is statically scoped, can have global variables

YUCK: destroys functional model, messes up structure sharing

Let expression

fortunately, Scheme provides a "clean" mechanism for creating variables to store (immutable) values

```
(let ((VAR1 VALUE1)
      (VAR2 VALUE2)
      . . .
      (VARn VALUEn))
  EXPRESSION)
```

let expression introduces a new environment with variables (i.e., a block)

good for naming a value (don't need `set!`)

a let expression has the same effect as creating a help function & passing value

as long as destructive assignments are not used, the functional model is preserved

- in particular, structure sharing is safe

```
(let ((x 5) (y 10))
  (let (z (x + y))
  )
)
```

environment where z = 15

environment where x = 5 and y = 10

Example: circle of friends

suppose we want to compute a person's circle of friends

- level 1: direct friends
- level 2: direct friends + friends of direct friends

  ...
- level n : level (n-1) friends + friends of level (n-1) friends

```
(define FRIENDS
  '((amy (bob dan elle)) (bob (amy dan)) (chaz (dan elle))
    (dan (chaz)) (elle (amy bob chaz dan)) (fred (dan))))

(define (getFriends person)
  (cadr (assoc person FRIENDS)))

(define (getCircle person distance)
  (if (= distance 1)
      (getFriends person)
      (let ((circle (getCircle person (- distance 1))))
        (append circle (apply append (map getFriends circle))))))
```

Example: circle of friends (cont.)

consider Amy's circle of friends

- level 1: (bob dan elle)
- level 2: (bob dan elle) + (amy dan) + (chaz) + (amy bob chaz dan) → (bob dan elle amy dan chaz amy bob chaz dan)

```
(require scheme/list)

(define FRIENDS
  '((amy (bob dan elle)) (bob (amy dan)) (chaz (dan elle))
    (dan (chaz)) (elle (amy bob chaz dan)) (fred (dan))))

(define (getFriends person)
  (cadr (assoc person FRIENDS)))

(define (getCircle person distance)
  (if (= distance 1)
      (getFriends person)
      (let ((circle (getCircle person (- distance 1))))
        (remove person
                (remove-duplicates (append circle
                                           (apply append
                                                  (map getFriends circle))))))))
```

don't list self in circle of friends

don't list duplicates in circle of friends

Example: craps simulation

consider a game of craps:

- if first roll is 7, then WINNER
- if first roll is 2 or 12, then LOSER
- if neither, then first roll is "point"
  – keep rolling until get 7 (LOSER) or point (WINNER)

```
(define (craps)

  (define (roll-until point)
    (let ((next-roll (+ (random 6) (random 6) 2)))
      (cond ((= next-roll 7) 'LOSER)
            ((= next-roll point) 'WINNER)
            (else (roll-until point)))))

  (let ((roll (+ (random 6) (random 6) 2)))
    (cond ((or (= roll 2) (= roll 12)) 'LOSER)
          ((= roll 7) 'WINNER)
          (else (roll-until roll)))))
```

Example: craps with history list

as is, all you see from `craps` is WINNER or LOSER

- would like to see the actual rolls to confirm proper behavior

the "functional way" is to construct a list of the rolls & return it

```
(define (craps)

    (define (roll-until point)
      (let ((next-roll (+ (random 6) (random 6) 2)))
        (cond ((= next-roll 7) (list next-roll 'LOSER))
              ((= next-roll point) (list next-roll 'WINNER))
              (else (cons next-roll (roll-until point))))))

    (let ((roll (+ (random 6) (random 6) 2)))
      (cond ((or (= roll 2) (= roll 12)) (list roll 'LOSER))
            ((= roll 7) (list roll 'WINNER))
            (else (cons roll (roll-until roll))))))
```

Example: craps with I/O

alternatively, can bite the bullet and use non-functional features

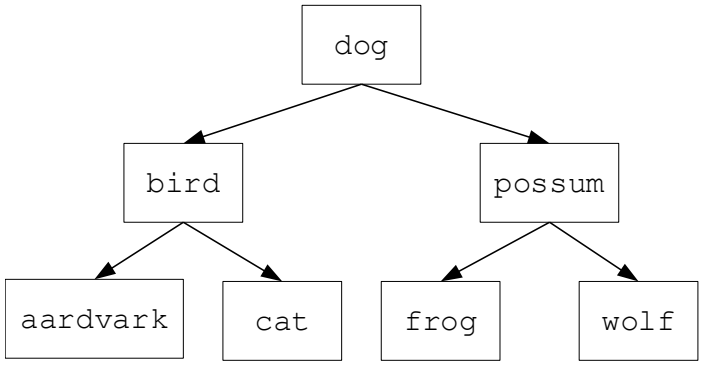
- `display` displays S-expr (`newline` yields carriage return)
- `read` reads S-expr from input
- `begin` provides sequencing (for side effects)

```
(define (craps)

  (define (roll-until point)
    (let ((next-roll (+ (random 6) (random 6) 2)))
      (begin (display "Roll: ")(display next-roll) (newline)
             (cond ((= next-roll 7) 'LOSER)
                   ((= next-roll point) 'WINNER)
                   (else (roll-until point))))))

  (let ((roll (+ (random 6) (random 6) 2)))
    (begin (display "Point: ") (display roll) (newline)
           (cond ((or (= roll 2) (= roll 12)) 'LOSER)
                 ((= roll 7) 'WINNER)
                 (else (roll-until roll))))))
```

Non-linear data structures

note: can represent non-linear structures using lists

e.g. trees



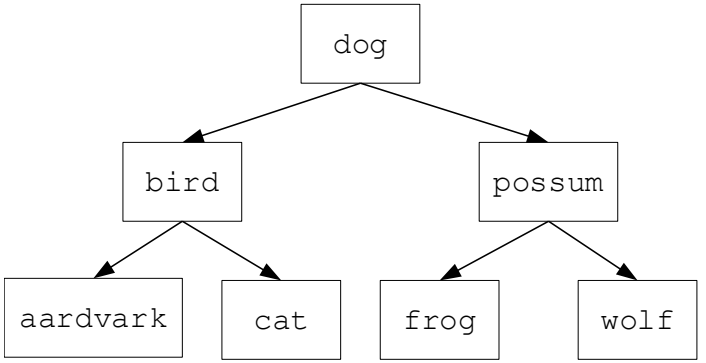

```
(dog
  (bird (aardvark () ()) (cat () ()))
  (possum (frog () ()) (wolf () ())))
```

- empty tree is represented by the empty list: `()`
- non-empty tree is represented as a list: `(ROOT LEFT-SUBTREE RIGHT-SUBTREE)`
- can access the the tree efficiently

```
(car TREE)    → ROOT
(cadr TREE)   → LEFT-SUBTREE
(caddr TREE)  → RIGHT-SUBTREE
```

Tree routines

```
(define TREE1
    ' (dog
       (bird (aardvark () ()) (cat () ()))
       (possum (frog () ()) (wolf () ()))))
```




```
(define (empty-tree? tree)
  (null? tree))

(define (root tree)
  (if (empty-tree? tree)
      'ERROR
      (car tree)))

(define (left-subtree  tree)
  (if (empty-tree? tree)
      'ERROR
      (cadr tree)))
```

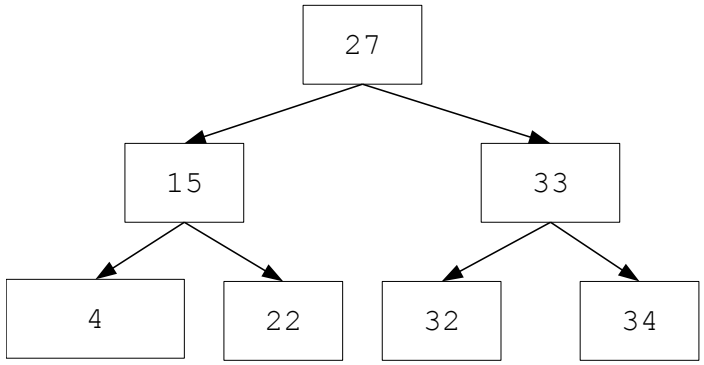
```
(define (right-subtree tree)
  (if (empty-tree? tree)
      'ERROR
      (caddr tree)))
```

Tree searching

note: can access root & either subtree in constant time

→ can implement binary search trees with O(log N) access

binary search tree: for each node, all values in left subtree are <= value at node
all values in right subtree are > value at node




```
(define (bst-contains? bstree sym)
  (cond ((empty-tree? bstree) #f)
        ((= (root bstree) sym) #t)
        ((> (root bstree) sym) (bst-contains? (left-subtree bstree) sym))
        (else (bst-contains? (right-subtree bstree) sym))))
```

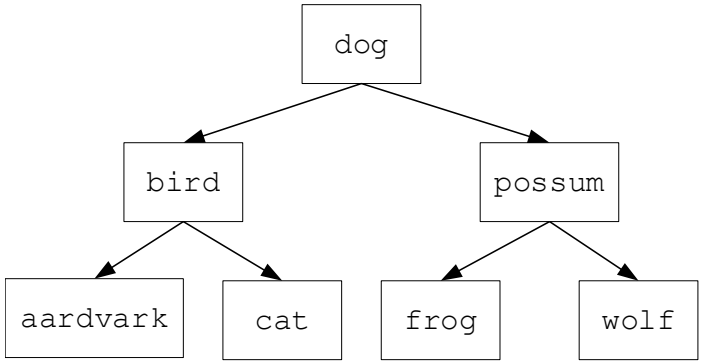
note: recursive nature of trees makes them ideal for recursive traversals

Tree traversal

```
(define (pre-order tree)
  (if (empty-tree? tree)
      '()
      (append (list (car tree))
              (pre-order (cadr tree))
              (pre-order (caddr tree)))))
```

```
(define (in-order tree)
  (if (empty-tree? tree)
      '()
      (append (in-order (cadr tree))
              (list (car tree))
              (in-order (caddr tree)))))
```

```
(define (post-order tree)
  (if (empty-tree? tree)
      '()
      (append (post-order (cadr tree))
              (post-order (caddr tree))
              (list (car tree)))))
```



- pre-order traversal?
- in-order traversal?
- post-order traversal?

In class exercises

```
(define (num-nodes tree)
    ??? )
```

```
(define (sum-values numtree)
    ??? )
```

```
(define (max-value numtree)
    ??? )
```