



Subprogram-level concurrency

a *task* or *process* or *thread* is a program unit that can be in concurrent execution with other program units

tasks differ from ordinary subprograms in that:

- a task may be implicitly started
- when a program unit starts the execution of a task, it is not necessarily suspended
- when a task's execution is completed, control may not return to the caller

tasks can be:

- heavyweight each executes in its own address space
- lightweight all tasks execute in the same address space (more efficient)

since tasks are rarely disjoint, there must be mechanisms for coordinating or synchronizing tasks

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	here, Buffer contains an array of ints
ublic class Buffer {	 will treat as a circular queue
<pre>private int [] buffer; private int numStored, putIndex, getIndex;</pre>	 putIndex will keep track of next place to put a value (wraps around)
<pre>public Buffer(int size) { this.buffer = new int[size]; }</pre>	 getIndex will keep track of next place to get a value (wraps around)
<pre>public synchronized void put(int task) { while(this.numStored == this.buffer.length) { true (void ())</pre>	 numStored keeps track of number currently stored
<pre>cly { wal(); } catch (InterruptedException e) { } }</pre>	useful Thread methods
<pre>this.buffer[this.putIndex] = task; this.putIndex =</pre>	 start() spawns the thread (i.e., calls its run method)
<pre>this.numStored++; notify(); }</pre>	 wait() suspends the current thread (and releases the monitor)
<pre>public synchronized int get() { while (this.numStored == 0) { try { wait(); } }</pre>	 notify() wakes up a thread waiting for the monitor
<pre>catch (InterruptedException e) { } } int task = this.buffer[this.getIndex]; this.getIndex = (this.getIndex + 1) % this.buffer.length;</pre>	<pre>public static void main(String [] args) { Buffer b = new Buffer(4); Producer p = new Producer(b); Consumer c = new Consumer(b);</pre>
<pre>this.numStored; notify(); return task;</pre>	<pre>p.start(); c.start(); }</pre>











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Example: parallel mergeSort

```
public class SortThread extends Thread {
  private int[] nums;
  private int minIndex;
  private int maxIndex;
  private int threadCount;
  public SortThread(int[] nums, int minIndex, int maxIndex, int threadCount) {
   this.nums = nums;
    this.minIndex = minIndex;
    this.maxIndex = maxIndex;
    this.threadCount = threadCount;
  1
 public void run() {
   MergeSort.mergeSortConcurrently(this.nums, this.minIndex,
                                         this.maxIndex, this.threadCount);
  }
}
```

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Example: parallel mergeSort public class MergeSort { public static void mergeSortConcurrently(int[] a, int threadCount) { MergeSort.mergeSortConcurrently(a, 0, a.length-1, threadCount); } public static void mergeSortConcurrently(int[] a, int minIndex, int maxIndex, int threadCount) { if (minIndex < maxIndex) {</pre> int mid = (minIndex+maxIndex)/2; if (threadCount > 1) { Thread leftThread = new SortThread(a, minIndex, mid, threadCount/2); Thread rightThread = new SortThread(a, mid+1, maxIndex, threadCount/2); leftThread.start(); rightThread.start(); try { leftThread.join(); rightThread.join(); } catch (InterruptedException ie) {} else { MergeSort.mergeSortConcurrently(a, minIndex, mid, threadCount/2); MergeSort.mergeSortConcurrently(a, mid+1, maxIndex, threadCount/2); MergeSort.merge(a, minIndex, maxIndex); } } 24

Example: parallel mergeSort

```
public static void main(String[] args) {
    Random randy = new Random();
    int size = 1000;

    System.out.println("Enter the thread limit: ");
    Scanner input = new Scanner(System.in);
    int numThreads = input.nextInt();
    input.close();

    while (true) {
        int[] nums = new int[size];
        for (int j = 0; j < size; j++) {
            nums[j] = randy.nextInt();
        }
        long start = System.currentTimeMillis();
        MergeSort.mergeSortConcurrently(nums, numThreads);
        long end = System.currentTimeMillis();
        System.out.printf("%10d elements => %6d ms \n", size, end-start);
        size *= 2;
    }
    }
}
```

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